Bounded-Deducibility Security: Reasoning About Information-Flow Security in a Fine-Grained Manner

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ITP 2021

29 June, 2021

ITP & I

ITP & **I**

datatypes hol types cosmed higher-order security consistency support standard sets integration isabelle proof formalization definitions case coinductive theory consistent including recursion type logic co constructors new codatatypes definition paper general

Isabelle & I



Isabelle view from Urbana, IL

Isabelle & I



Isabelle view from Urbana, IL



Isabelle view from Munich

In This Talk

Verification of information flow security of multi-user, web-based systems

Fine-grained coverage of the (dis)allowed flows

General framework for specifying and verifying such systems

Experience with deploying one such system "in the wild"

In This Talk

1 Introduction

- **2** Bounded-Deducibility (BD) Security
- **3** CoCon's Verification
- **4** CoCon in the Wild
- **5** Other Applications and Developments of BD Security

Contributors to the Work Presented Here



Thomas Bauereiss



Peter Lammich

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Thomas Bauereiss



Peter Lammich



Sergey Grebenshchikov



Ping Hou



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Armando Pesenti Gritti



Franco Raimondi

EasyChair, the most popular conference management system

HotCRP, the second most popular one

EasyChair, the most popular conference management system It is our pleasure to inform you that your paper has been accepted to the IEEE Symposium of Security and Privacy (Oakland) 2012. Out of 307 submitted papers, we accepted 40 papers.

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How can they go wrong? Confidentiality and integrity violations

CoCon

CoCon = Feature-rich conference management system (similar to EasyChair and HotCRP)

Welcome to CoCon.

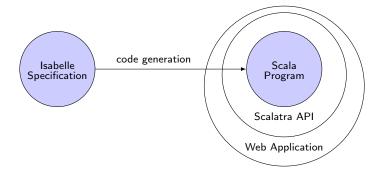
CoCon is a conference management system with verified document confidentiality. What makes CoCon special compared to other conference systems is that it is **built around a verified core that is guaranteed not to leak**. Of course, the non-leakage of the overall system relies on a number of assumptions, such as the soundness of the proof assistant. Moreover, there is a thin layer of critical code between the verified core and the frontend that must be trusted.



New user? Sign up here	
Email	
Full name	
Affiliation	
Password	
Password (confirmation)	
Sign up	



CoCon's Architecture





Information does not leak from CoCon's kernel.



CoCon's Verification

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A user learns nothing about a paper's content beyond the last submitted version unless they become an author of the paper.

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Source of Secrets Observations Bound Trigger

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Bounded Deducibility (BD) Security

O can learn nothing about S beyond B unless T occurs.

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4 CoCon in the Wild

5 Other Applications and Developments of BD Security

 $\mathsf{SysTrace} \subseteq \mathsf{List}(\mathsf{Event})$

SysTrace

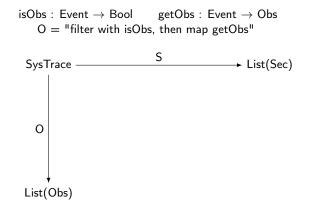
List(Sec)

List(Obs)

 $SysTrace \subseteq List(Event)$

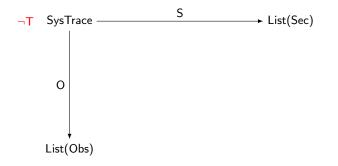
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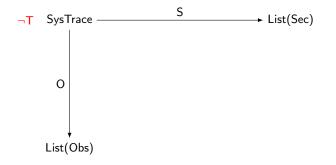
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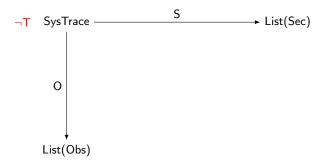


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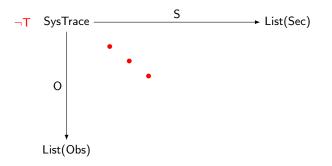
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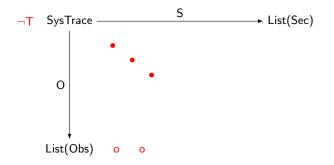
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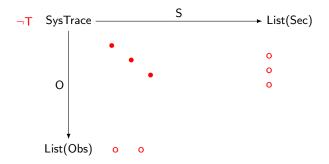
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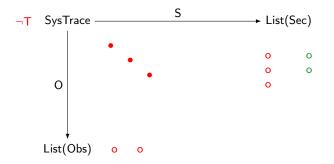
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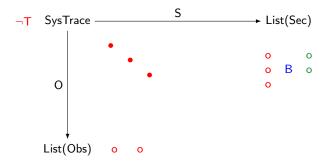
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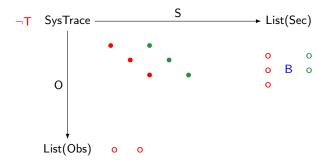
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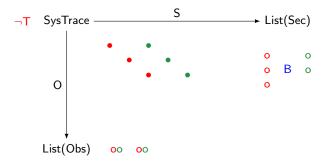
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Formal Definition of BD Security

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A flow policy \mathcal{F} for \mathcal{A} consists of:

- an observation infrastructure (Obs, isObs, getObs)
- a secrecy infrastructure (Sec, isSec, getSec)
- a declassification bound $\mathsf{B}:\mathsf{List}(\mathsf{Sec})\to\mathsf{List}(\mathsf{Sec})\to\mathsf{Bool}$
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 \mathcal{A} being BD secure w.r.t. \mathcal{F} , written $\mathcal{A} \models \mathcal{F}$, means: For all $tr_1 \in SysTrace$ and $sl_1, sl_2 \in List(Sec)$, if never T tr_1 , S $tr_1 = sl_1$ and B $sl_1 sl_2$, then there exists $tr_2 \in SysTrace$ with O $tr_2 = O tr_1$ and S $tr_1 = sl_1$. (where never T tr_1 means "T holds for no event in tr_1 ")

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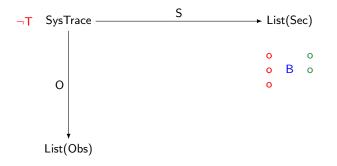
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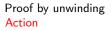
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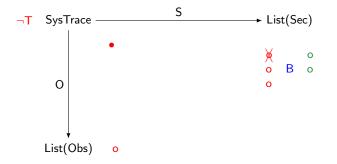
Traditional unwinding: safety-like property

Unwinding for BD security: safety + liveness

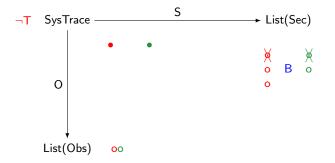
Proof by unwinding

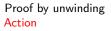


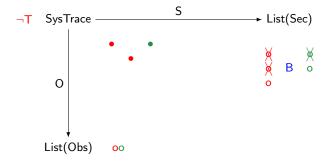


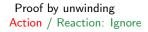


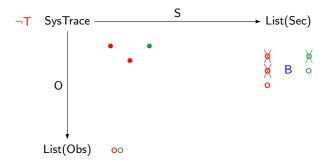


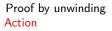


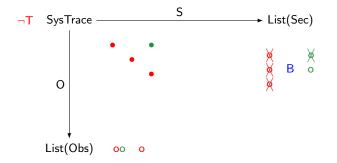




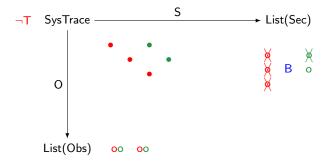


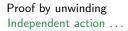


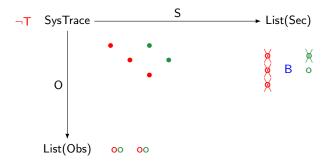


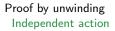


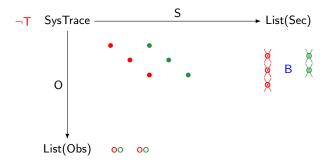


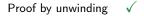


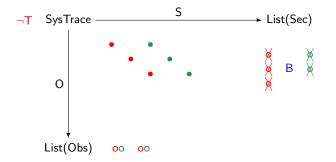


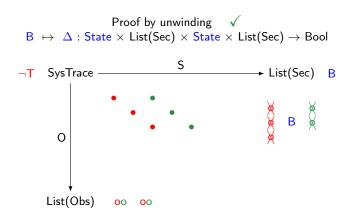












$\Delta: \mathsf{State} \times \mathsf{List}(\mathsf{Sec}) \times \mathsf{State} \times \mathsf{List}(\mathsf{Sec}) \to \mathsf{Bool}$

```
\begin{array}{l} \Delta: {\tt State} \times {\tt List}({\tt Sec}) \times {\tt State} \times {\tt List}({\tt Sec}) \rightarrow {\tt Bool} \\ + \\ {\tt Strategy for:} \\ {\tt when to act independently} \\ {\tt when to react} \\ {\tt if react: when to match and when to ignore} \end{array}
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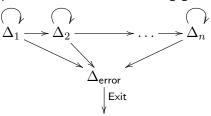
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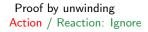
split unwinding relation into components have "error" component to exit the unwinding game ASAP

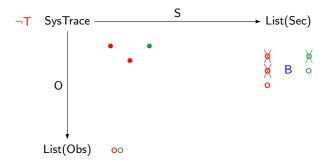
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Bounded-Deducibility (BD) Security

Takes an Epistemic (Knowledge) Logic perspective to information flow

Generalizes Nondeducibility (Sutherland 1986)

Related notions: Secrecy Maintenance (Halpern and O'Neill 2008) and Gradual Release (Askarov & Sabelfeld 2007)

BD Unwinding generalizes the standard unwinding proof method (Goguen & Meseguer 1984, Mantel 2003)

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CoCon's Verified Confidentiality Properties

All formulated as instances of BD Security

All verified using BD Unwinding

Secret	Trigger	Bound
Paper Content	Paper Authorship	Last Uploaded Version
	Paper Authorship or PC Membership ^B	Nothing
		Last Edited Version
Review	Review Authorship	Before Discussion and
		All the Later Versions
	Review Authorship or	Last Edited Version
	Non-Conflict PC Membership ^D	Before Notification
	Review Authorship or	
	Non-Conflict PC Membership ^D or	Nothing
	Paper Authorship ^N	
Discussion	Non-Conflict PC Membership	Nothing
Decision	Non-Conflict PC Membership	Last Edited Version
	Non-Conflict PC Membership or PC Membership ^N or Paper Authorship ^N	Nothing
Reviewer		Non-Conflict PC Membership
Assignment	Non-Conflict PC Membership ^R	of Reviewers
to Paper		
	Non-Conflict PC Membership ^R or	Non-Conflict PC Membership
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Overall Verification Effort 🥔

BD Security framework: 1000 LOC

Confidentiality properties: 5000 LOC

Safety properties: 1000 LOC

Traceback properties: 700 LOC

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Safety properties: 1000 LOC 2. And authors are always in conflict with their papers $(1) + (2) \rightarrow$ Authors never learn such and such Traceback properties: 700 LOC

Overall Verification Effort 🥔

BD Security framework: 1000 LOC

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But how can one become such and such?

E.g., how could $\mathbf{\hat{m}}$ become an author of $\mathbf{\hat{m}}$?

But how can one become such and such?

E.g., how could $\mathbf{\hat{m}}$ become an author of $\mathbf{\hat{l}}$?



But how can one become such and such?

E.g., how could $\mathbf{\hat{T}}$ become an author of $\mathbf{\hat{E}}$?

But how can one become such and such?

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E.g., how could $\mathbf{\hat{m}}$ become an author of $\boldsymbol{\mathbb{B}}$?



 $\mathsf{Confidentiality} + \mathsf{Safety} + \mathsf{Traceback} \Longrightarrow \mathsf{Relax}$

Some Trivia

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"The authors cunningly chose a topic that directly speaks to the reviewers of their paper."

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CoCon has a superuser called "The Voronkov" to acknowledge CoCon's inspiration from EasyChair.

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CoCon in the Wild

CoCon has been used to manage two international conferences:

TABLEAUX 2015: The 24th Conference on Automated Reasoning with Analytic Tableaux and Related Methods

ITP 2016: The 7th Conference on Interactive Theorem Proving (29th if we count its predecessor conference)



Hans de Nivelle conference chair



Hans de Nivelle conference chair

CoCon?? At TABLEAUX 2015?? Not a chance!



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But maybe CoCon++...

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CoCon plus the following features:

Various convenience listings, e.g.: OK

- For PC members: papers listed by average score
- For the chair: paper load of each PC, reviewer number for each paper

Email notifications: OK, if done right

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Is CoCon++ as secure as CoCon?

We proved that it is!

On the way: designed framework for secure system extensions.

Had proved about CoCon's kernel:

An author learns nothing about the score of their paper before notification.



I'm also an author and I see my paper listed somewhere in the middle. Does it mean I can already infer something about its score?

TABLEAUX PC member in Discussion phase

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I'm also an author and I see my paper listed somewhere in the middle. Does it mean I can already infer something about its score?

TABLEAUX PC member in Discussion phase

No, that was only a pseudo-leak.

Web interface written around the verified kernel – web developer decided to treat score "unknown" as 0 when sorting papers by score to display to a user.



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Jasmin Blanchette conference co-chair

Announcement: The 7th International Conference on Interactive Theorem Proving 22 to 26 August 2016, Nancy, France

Papers should be submitted in PDF format via EasyChair.



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My email message to Jasmin: Traitor!

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Me: No hard feelings; in fact, it would've been a huge amount of stress for me.
Jasmin: In that case, it could be fun. Maybe we should go with CoCon.

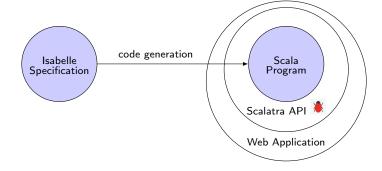


Andrew Tolmach PC member

I'm a little nervous that some unintended leakage may be occurring! ... why did I see the scores of a paper I have conflict with?

What Had Happened?

CoCon's Architecture



Critical Data Race Bug Outside the Verified Kernel

Why have we not discovered it

- during heavy testing
- during countless conference simulations
- during TABLEAUX 2015

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Because it occurs very seldom

- Needs sufficient delays (caused by high traffic)
- Is volatile: happens per single request, then vanishes

Critical Data Race Bug Outside the Verified Kernel

Why have we not discovered it

- during heavy testing
- during countless conference simulations
- during TABLEAUX 2015 70 users
 ITP 2016 110 users

Because it occurs very seldom

- Needs sufficient delays (caused by high traffic)
- Is volatile: happens per single request, then vanishes

What were the consequences?

What we verified for the kernel was compromised by the API layer.

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However

- Due to rarity and volatilily, users would not notice
- Really sensitive data was at least two clicks away
- Authors and PC members were accessing the system at different times

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However

- Due to rarity and volatilily, users would not notice
- Really sensitive data was at least two clicks away
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The bug was fixed during the discussion phase.

Andrew Tolmach:

IMO, the whole episode is an unusually clear illustration of the perils of overselling (even to oneself) the benefits of verification. The most interesting thing is not that CoCon had a bug, but rather that the developers were (temporarily) in denial about it. The most revealing pieces of the email exchange over the bug were the following from Andrei in response to my bug report:

> A leak is impossible this way: such information does not leak through the kernel.

and a little later:

> Again, I am not sure what is going on, but I am sure that it is not a leak. The server is accessed with your credentials, and the scores of reviews of conflicted papers are not accessible with your credentials.

Lessons Learned

Unverified part deserves special attention

- Large effort verifying the kernel's rich information flow
- Not enough effort in reviewing carefully the thin outer layer

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- Large effort verifying the kernel's rich information flow
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Some discussion on extending CoCon's verification to the outer layers.

Important to always state precisely which part of the system was verified – even in a summary!

Before ITP 2016

Welcome to CoCon.

CoCon is a conference management system with verified document confidentiality. What makes CoCon special compared to other conference systems is the fact that **quite certainly it does not leak**.



Forgot your password

New user? Sign up here	
Email	
Full name	
Affiliation	
Password	
Password (confirmation)	
Sign up	

After ITP 2016

Welcome to CoCon.

CoCon is a conference management system with verified document confidentiality. What makes CoCon special compared to other conference systems is that it is **built around a verified core that is guaranteed not to leak**. Of course, the non-leakage of the overall system relies on a number of assumptions, such as the soundness of the proof assistant. Moreover, there is a thin layer of critical code between the verified core and the frontend that must be trusted.

Learn more »			

Sign in to CoCon	
Email	
Sign in	Forgot your
New user? Sign up here	
Email	
Full name	
Affiliation	
Password	
Password (confirmation)	
Sign up	

More Details on CoCon's Verification and Deployment Saga

Andrei Popescu, Peter Lammich, Ping Hou.

CoCon: A Conference Management System with Formally Verified Document Confidentiality.

Journal of Automated Reasoning 2021

1 Introduction

2 Bounded-Deducibility (BD) Security

3 CoCon's Verification

4 CoCon in the Wild

5 Other Applications and Developments of BD Security

CoSMed

Facebook-style social media platform

- users register, create posts (which can later be updated) and establish friendship relationships
- post access can be public or friends-only (and this can change) Implemented using the same scheme as CoCon

- Bound: complete nondeducibility
- Trigger: Acquisition of various roles or the opening of access

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Too weak

Bound: complete nondeducibility

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Too weak

Better justice to what's going on (stronger confidentiality property):

A group of users learn about a post nothing beyond the updates performed while (or last before) one of them is the admin, or is the post's owner, or becomes friends with the owner, or the post is marked as public.

Bound: complete nondeducibility

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inductive bound \mathbb{B}

CoSMed – Proved Confidentiality Properties

Secret	(Trigger-Swallowing) Bound
	Updates performed while or last before
	one of the following holds:
Content of a siven next	– Some user in G is the admin,
Content of a given post	is the post owner
	or is friends with its owner
	 The post is marked as public
	Status changes performed while or last before
Friendship status between	the following holds:
two given users U and V	– Some user in G is the admin
	or is friends with U or V
	Existence of accepted requests while or last before
Friendship requests between	the following holds:
two given users U and V	– Some user in G is the admin
	or is friends with U or V

The observations are made by a group of users G. The trigger is vacuously false.

Bauereiss, Pesenti Gritti, Popescu, Raimondi. CoSMed: A Confidentiality-Verified Social Media Platform. ITP 2016, JAR 2018.

CoSMeDis

Diaspora-style extension of CosMed:

- multiple CosMed nodes deployed at different sites
- any two nodes can connect: posts can be shared and friendships can be established cross-nodes

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Question: Do CosMed's confidentiality guarantees extend to CoSMeDis?

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- multiple CosMed nodes deployed at different sites
- any two nodes can connect: posts can be shared and friendships can be established cross-nodes

Question: Do CosMed's confidentiality guarantees extend to CoSMeDis?

Broader research question: How to compose BD Security flow policies of individual nodes to form guarantees for the entire network?

Rough Statement of the Theorem. If n communicating systems (e.g., n CoSMeDis nodes) have their communication:

- observable to a sufficient degree, and
- secret-polarized (i.e., only of the nodes issues the secrets of interest),

and each of them satisfies a BD security policy \mathcal{F}_i , then their communicating product satisfies a naturally defined product policy $\prod_{i=1}^{n} \mathcal{F}_i$.

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Weakness: Restriction on communicating with only one secret source.

Applied to lift CoSMed's confidentiality guarantees to CoSMeDis.

Bauereiss, Pesenti Gritti, Popescu, Raimondi. CoSMeDis: A Distributed Social Media Platform with Formally Verified Confidentiality Guarantees. IEEE Symposium on Security and Privacy, 2017

Confidentiality Properties Lifted from CoSMed to CoSMeDis

Secret	Bound
	Updates performed while or last before
	one of the following holds:
	– Some user in G_i is the node's admin,
Content of a given post at node i	is the post owner
Content of a given post at node i	or is friends with its owner
	 The post is marked as public
	– Some user in G_j for $j \neq i$ is the admin at node j
	or is remote friends with the post's owner
	Status changes performed while or last before
Friendship status between	the following holds:
two given users U and V at node i	 Some user at node i is the node's admin
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Friendship requests between	the following holds:
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The observations are made by n groups of users—one group G_i at each node i. The declassification trigger is again vacuously false.

Framework for expressing and verifying fine-grained information flow security properties

Formalized in Isabelle/HOL

Comes with mechanisms for managing complexity: compositional incremental proof machinery, compositionality results

Fine-tuned on some large verification projects: CoCon, CoSMed, CoSMeDis

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Try it today for free (available from the Isabelle AFP)

More Related/Relevant/Inspiring Work

Systems verified for information-flow security: hardware architecture with information flow primitives (Amorim et al.), an ARM-based separation kernel (Dam et al.), noninterference for seL4 (Murray et al.), the Quark verified browser (Jang et al.)

Automatic analysis of information flow security: Jif/Fabric (Myers, Liu et al.), LIO/Hails (Giffin et al.), Paragon (Broberg et al.), Jeeves (Yang at al.) and Ur/Web (Chlipala).

Information Flow Security for Conference Management Systems: ConfiChair (Arapinis et al.), Qapla (Mehta et al.)

Temporal logic approaches: SecLTL (Dimitrova et al.), HyperLTL (Clarkson et al.)

Compositionality results: McCullough's early work, Mantel's MAKS

Bounded-Deducibility Security. ITP 2021



Popescu, Lammich, Hou. CoCon: A Conference Management System with Formally Verified Document Confidentiality. Journal of Automated Reasoning, 2021.

Bauereiss, Pesenti Gritti, Popescu, Raimondi. CoSMed: A Confidentiality-Verified Social Media Platform. Journal of Automated Reasoning, 2018. (Journal version of ITP 2016 paper)

Bauereiss, Pesenti Gritti, Popescu, Raimondi. CoSMeDis: A Distributed Social Media Platform with Formally Verified Confidentiality Guarantees. IEEE Symposium on Security and Privacy, 2017.

Kanav, Lammich, Popescu. A Conference Management System with Verified Document Confidentiality. CAV 2014.

Support from DFG (through RS³), EPSRC and NCSC/VeTSS gratefully acknowledged.

Reserve Slides

Secret	Trigger	Bound
Paper Content	Paper Authorship	Last Uploaded Version
	Paper Authorship or PC Membership ^B	Nothing
		Last Edited Version
Review	Review Authorship	Before Discussion and
		All the Later Versions
	Review Authorship or	Last Edited Version
	Non-Conflict PC Membership ^D	Before Notification
	Review Authorship or	
	Non-Conflict PC Membership ^D or	Nothing
	Paper Authorship ^N	
Discussion	Non-Conflict PC Membership	Nothing
Decision	Non-Conflict PC Membership	Last Edited Version
	Non-Conflict PC Membership or PC Membership ^N or Paper Authorship ^N	Nothing
Reviewer		Non-Conflict PC Membership
Assignment	Non-Conflict PC Membership ^R	of Reviewers
to Paper		
	Non-Conflict PC Membership ^R or	Non-Conflict PC Membership
	Paper Authorship ^N	of Reviewers

Phase Stamps: B = Bidding, D = Discussion, N = Notification, R = Review

A group of users UIDs learns nothing about the content of a paper's review (say, review N of paper PID) beyond the last submitted version before the discussion phase and the later versions unless one of them is that review's author.

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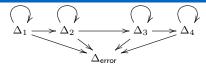
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Bound: Two lists of secrets, which are lists of pairs phase-update, are related by B iff:

their suffixes consisting of pairs having phase Discussion are equal, and their last updates before those suffixes are also equal.



		$\bigcap_{A_1} \bigcap_{A_2} \bigcap_{A_3} \bigcap_{A_4} \bigcap_{A$
		$\Delta_1 \longrightarrow \Delta_2 \longrightarrow \Delta_3 \longrightarrow \Delta_4$ $\Delta_{\text{error}} \Delta_4$
ſ		
	$\Delta_1\left(\sigma_1, \textit{sl}_1, \sigma_2, \textit{sl}_2\right)$	$(\forall cid. \ PID \in paperIDs \ \sigma_1 \ cid \to phase \ \sigma_1 \ cid < Reviewing) \land \\ \sigma_1 = \sigma_2 \land B \ sl_1 \ sl_2$
	$\Delta_2 \left(\sigma_1, \textit{sl}_1, \sigma_2, \textit{sl}_2 \right)$	$\begin{array}{l l} (\exists cid. & PID \in paperIDs \ \sigma_1 \ cid \ \land \ phase \ \sigma_1 \ cid = Reviewing \ \land \\ \neg \ (\exists uid. \ isRevNth \ \sigma_1 \ uid \ PID \ N)) \ \land \\ \sigma_1 = \sigma_2 \ \land \ B \ sl_1 \ sl_2 \end{array}$
	$\Delta_3 \left(\sigma_1, \textit{sl}_1, \sigma_2, \textit{sl}_2 \right)$	$ \begin{array}{c} (\exists \mathit{cid} \ \mathit{uid}. \ PID \in paperIDs \ \sigma_1 \ \mathit{cid} \wedge phase \ \sigma_1 \ \mathit{cid} = Reviewing \ \land \\ \\ \hline isRevNth \ \sigma_1 \ \mathit{uid} \ PID \ N \end{array}) \ \land \\ \\ \sigma_1 =_{PID,N} \ \sigma_2 \ \land B \ \mathit{sl}_1 \ \mathit{sl}_2 \end{array} $
	$\Delta_4 \left(\sigma_1, \textit{sl}_1, \sigma_2, \textit{sl}_2 ight)$	$ \begin{array}{l} (\exists \mathit{cid} \ \mathit{uid}. \ PID \in paperIDs \ \sigma_1 \ \mathit{cid} \land \ phase \ \sigma_1 \ \mathit{cid} \geq Reviewing \ \land \\ \\ isRevNth \ \sigma_1 \ \mathit{uid} \ PID \ N) \land \\ \\ \sigma_1 = \sigma_2 \ \land (\ \exists \mathit{wl}. \ \mathit{sl}_1 = \mathit{sl}_2 = map \ (Pair \ Discussion) \ \mathit{wl} \) \end{array} $
	$\Delta_{error}\left(\sigma_{1}, \mathit{sl}_{1}, \sigma_{2}, \mathit{sl}_{2} ight)$	$ \begin{split} sl_1 \neq [] \land \\ ((\exists cid. \ PID \in paperIDs \ \sigma_1 \ cid \land phase \ \sigma_1 \ cid > Reviewing \land \\ \neg \ (\exists uid. \ isRevNth \ \sigma_1 \ uid \ PID \ N)) \\ \lor \\ (\exists cid. \ PID \in paperIDs \ \sigma_1 \ cid \land phase \ \sigma_1 \ cid > Reviewing \land \\ fst \ (hd \ sl_1) = Reviewing)) \end{split} $

		$\bigcap_{\Delta_1} \Delta_2 \Delta_3 \Delta_4$
		Aerror
4	$\Delta_1 \left(\sigma_1, \textit{sl}_1, \sigma_2, \textit{sl}_2 ight)$	$(\forall cid. PID \in paperIDs \ \sigma_1 \ cid \to phase \ \sigma_1 \ cid < Reviewing) \land \sigma_1 = \sigma_2 \land B \ sl_1 \ sl_2$
4	$\Delta_2\left(\sigma_1, extsf{sl}_1, \sigma_2, extsf{sl}_2 ight)$	$\begin{array}{l l} (\exists cid. \ PID \in paperIDs \ \sigma_1 \ cid \ \land \ phase \ \sigma_1 \ cid = Reviewing \ \land \\ \neg \ (\exists uid. \ isRevNth \ \sigma_1 \ uid \ PID \ N)) \ \land \\ \sigma_1 = \sigma_2 \ \land \ B \ sl_1 \ sl_2 \end{array}$
4	$\Delta_{3}\left(\sigma_{1}, \textit{sl}_{1}, \sigma_{2}, \textit{sl}_{2} ight)$	$ \begin{array}{c} (\exists \mathit{cid} \ \mathit{uid}. \ PID \in paperIDs \ \sigma_1 \ \mathit{cid} \wedge phase \ \sigma_1 \ \mathit{cid} = Reviewing \ \land \\ \\ \hline isRevNth \ \sigma_1 \ \mathit{uid} \ PID \ N \end{array}) \ \land \\ \\ \sigma_1 =_{PID,N} \ \sigma_2 \ \land B \ \mathit{sl}_1 \ \mathit{sl}_2 \end{array} $
4	$\Delta_4 \left(\sigma_1, \textit{sl}_1, \sigma_2, \textit{sl}_2 ight)$	$ \begin{array}{l} (\exists \mathit{cid} \ \mathit{uid}. \ PID \in paperIDs \ \sigma_1 \ \mathit{cid} \land \ phase \ \sigma_1 \ \mathit{cid} \geq Reviewing \ \land \\ \\ isRevNth \ \sigma_1 \ \mathit{uid} \ PID \ N) \land \\ \\ \hline \sigma_1 = \sigma_2 \ \land (\ \exists \mathit{wl}. \ \mathit{sl}_1 = \mathit{sl}_2 = map \ (Pair \ Discussion) \ \mathit{wl} \) \end{array} $
4	$\Delta_{error} \left(\sigma_1, \mathit{sl}_1, \sigma_2, \mathit{sl}_2 ight)$	$ \begin{aligned} sI_1 \neq [] \land \\ ((\exists cid. \ PID \in paperIDs \ \sigma_1 \ cid \land phase \ \sigma_1 \ cid > Reviewing \land \\ \neg (\exists uid. \ isRevNth \ \sigma_1 \ uid \ PID \ N)) \\ \lor \\ (\exists cid. \ PID \in paperIDs \ \sigma_1 \ cid \land phase \ \sigma_1 \ cid > Reviewing \land \\ fst \ (hd \ sI_1) = Reviewing)) \end{aligned} $

	$\bigcap_{\Delta_1} \xrightarrow{\frown} \Delta_2 \xrightarrow{\frown} \Delta_3 \xrightarrow{\frown} \Delta_4$
	Δ_1 Δ_2 Δ_4 Δ_{error}
$\Delta_1 (\sigma_1, \mathit{sl}_1, \sigma_2, sl_2, sl$	$(\forall cid \text{ PID} \in \text{paperIDs } \sigma_1 \ cid \rightarrow \text{phase } \sigma_1 \ cid < \text{Reviewing}) \land$
$\Delta_2 (\sigma_1, \mathit{sl}_1, \sigma_2, \mathit{sl}_2)$	
$\Delta_3 \left(\sigma_1, \mathfrak{sl}_1, \sigma_2, \mathfrak{sl}_2 \right)$	
$\Delta_4 \left(\sigma_1, \mathit{sl}_1, \sigma_2, \mathit{s} \right)$	
$\Delta_{error} \left(\sigma_1, sl_1, \sigma_2 \right)$	$ sl_1 \neq [] \land \\ ((\exists cid. \ PID \in paperIDs \ \sigma_1 \ cid \land phase \ \sigma_1 \ cid > Reviewing \land \\ \neg (\exists uid. \ isRevNth \ \sigma_1 \ uid \ PID \ N)) \\ \lor \\ (\exists cid. \ PID \in paperIDs \ \sigma_1 \ cid \land phase \ \sigma_1 \ cid > Reviewing \land \\ fst \ (hd \ sl_1) = Reviewing)) $

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$\Delta_3 \left(\sigma_1, \textit{sl}_1, \sigma_2, \textit{sl}_2 ight)$	$ \begin{array}{c} (\exists \mathit{cid} \ \mathit{uid}. \ PID \in paperIDs \ \sigma_1 \ \mathit{cid} \wedge phase \ \sigma_1 \ \mathit{cid} = Reviewing \ \land \\ & isRevNth \ \sigma_1 \ \mathit{uid} \ PID \ N \end{array}) \ \land \\ \\ \sigma_1 =_{PID,N} \ \sigma_2 \ \land B \ \mathit{sl}_1 \ \mathit{sl}_2 \end{array} $
$\Delta_4 \left(\sigma_1, \textit{sl}_1, \sigma_2, \textit{sl}_2 ight)$	$ \begin{array}{l} (\exists \mathit{cid} \ \mathit{uid}. \ PID \in paperIDs \ \sigma_1 \ \mathit{cid} \land \ phase \ \sigma_1 \ \mathit{cid} \geq Reviewing \ \land \\ \\ isRevNth \ \sigma_1 \ \mathit{uid} \ PID \ N) \land \\ \\ \sigma_1 = \sigma_2 \ \land (\ \exists \mathit{wl}. \ \mathit{sl}_1 = \mathit{sl}_2 = map \ (Pair \ Discussion) \ \mathit{wl} \) \end{array} $
$\Delta_{error}\left(\sigma_{1}, \mathit{sl}_{1}, \sigma_{2}, \mathit{sl}_{2} ight)$	$ \begin{split} sl_1 \neq [] \land \\ ((\exists cid. \ PID \in paperIDs \ \sigma_1 \ cid \land phase \ \sigma_1 \ cid > Reviewing \land \\ \neg \ (\exists uid. \ isRevNth \ \sigma_1 \ uid \ PID \ N)) \\ \lor \\ (\exists cid. \ PID \in paperIDs \ \sigma_1 \ cid \land phase \ \sigma_1 \ cid > Reviewing \land \\ fst \ (hd \ sl_1) = Reviewing)) \end{split} $

		$\bigcap_{A_1} \bigcap_{A_2} \bigcap_{A_3} \bigcap_{A_4} \bigcap_{A$
		$\Delta_1 \longrightarrow \Delta_2 \longrightarrow \Delta_3 \longrightarrow \Delta_4$
		Δ_{error}
	$\Delta_1\left(\sigma_1, \textit{sl}_1, \sigma_2, \textit{sl}_2\right)$	$(\forall cid. \ PID \in paperIDs \ \sigma_1 \ cid \to phase \ \sigma_1 \ cid < Reviewing) \land \\ \sigma_1 = \sigma_2 \land B \ sl_1 \ sl_2$
Î	$\Delta_2\left(\sigma_1, \mathit{sl}_1, \sigma_2, \mathit{sl}_2 ight)$	$ \begin{array}{c c c c c c c c c c c c c c c c c c c $
	$\Delta_3 \left(\sigma_1, \textit{sl}_1, \sigma_2, \textit{sl}_2 ight)$	$ \begin{array}{c c} (\exists \mathit{cid} \ \mathit{uid}. \ PID \in paperIDs \ \sigma_1 \ \mathit{cid} \wedge phase \ \sigma_1 \ \mathit{cid} = Reviewing \ \land \\ \hline isRevNth \ \sigma_1 \ \mathit{uid} \ PID \ N \end{array}) \ \land \\ \hline \sigma_1 =_{PID,N} \ \sigma_2 \ \land B \ \mathit{sl}_1 \ \mathit{sl}_2 \end{array} $
ĺ	$\Delta_4 \left(\sigma_1, \textit{sl}_1, \sigma_2, \textit{sl}_2 ight)$	$ \begin{array}{l} (\exists \mathit{cid} \ \mathit{uid}. \ PID \in paperIDs \ \sigma_1 \ \mathit{cid} \land \ phase \ \sigma_1 \ \mathit{cid} \geq Reviewing \ \land \\ \\ isRevNth \ \sigma_1 \ \mathit{uid} \ PID \ N) \land \\ \\ \hline \sigma_1 = \sigma_2 \ \land (\ \exists \mathit{wl}. \ \mathit{sl}_1 = \mathit{sl}_2 = map \ (Pair \ Discussion) \ \mathit{wl} \) \end{array} $
	$\Delta_{error} \left(\sigma_1, \mathit{sl}_1, \sigma_2, \mathit{sl}_2 ight)$	$ \begin{split} sl_1 \neq [] \land \\ ((\exists cid. \ PID \in paperIDs \ \sigma_1 \ cid \land phase \ \sigma_1 \ cid > Reviewing \land \\ \neg \ (\exists uid. \ isRevNth \ \sigma_1 \ uid \ PID \ N)) \\ \lor \\ (\exists cid. \ PID \in paperIDs \ \sigma_1 \ cid \land phase \ \sigma_1 \ cid > Reviewing \land \\ fst \ (hd \ sl_1) = Reviewing)) \end{split} $

$\bigcap_{\Delta_1} \Delta_2 \Delta_3 \Delta_4$		
Δ_{error}		
	$\Delta_1 \left(\sigma_1, \textit{sl}_1, \sigma_2, \textit{sl}_2 \right)$	$(\forall cid. \ PID \in paperIDs \ \sigma_1 \ cid \to phase \ \sigma_1 \ cid < Reviewing) \land \\ \sigma_1 = \sigma_2 \land B \ sl_1 \ sl_2$
	$\Delta_2 \left(\sigma_1, \textit{sl}_1, \sigma_2, \textit{sl}_2 ight)$	$ \begin{array}{c c c c c c c c c c c c c c c c c c c $
0	$\Delta_3\left(\sigma_1, \textit{sl}_1, \sigma_2, \textit{sl}_2 ight)$	$ \begin{array}{c} (\exists \mathit{cid} \ \mathit{uid}. \ PID \in paperIDs \ \sigma_1 \ \mathit{cid} \wedge phase \ \sigma_1 \ \mathit{cid} = Reviewing \ \land \\ \\ \hline isRevNth \ \sigma_1 \ \mathit{uid} \ PID \ N \end{array}) \ \land \\ \\ \sigma_1 =_{PID,N} \ \sigma_2 \ \land B \ \mathit{sl}_1 \ \mathit{sl}_2 \end{array} $
	$\Delta_4 \left(\sigma_1, \textit{sl}_1, \sigma_2, \textit{sl}_2 ight)$	$ \begin{array}{l} (\exists \mathit{cid} \ \mathit{uid}. \ PID \in paperIDs \ \sigma_1 \ \mathit{cid} \land \ phase \ \sigma_1 \ \mathit{cid} \geq Reviewing \ \land \\ \\ isRevNth \ \sigma_1 \ \mathit{uid} \ PID \ N) \land \\ \hline \\ \sigma_1 = \sigma_2 \ \land (\ \exists \mathit{wl}. \ \mathit{sl}_1 = \mathit{sl}_2 = map \ (Pair \ Discussion) \ \mathit{wl} \) \end{array} $
	$\Delta_{error} \left(\sigma_1, \mathit{sl}_1, \sigma_2, \mathit{sl}_2 ight)$	$ \begin{split} sl_1 \neq [] \land \\ ((\exists cid. \ PID \in paperIDs \ \sigma_1 \ cid \land phase \ \sigma_1 \ cid > Reviewing \land \\ \neg \ (\exists uid. \ isRevNth \ \sigma_1 \ uid \ PID \ N)) \\ \lor \\ (\exists cid. \ PID \in paperIDs \ \sigma_1 \ cid \land phase \ \sigma_1 \ cid > Reviewing \land \\ fst \ (hd \ sl_1) = Reviewing)) \end{split} $